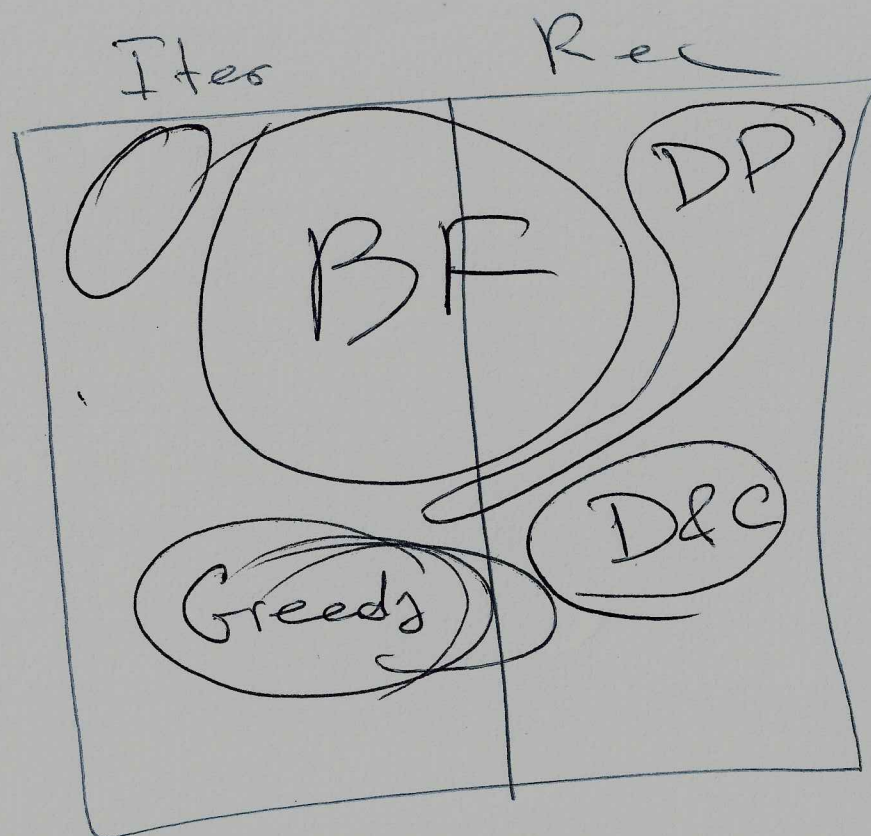


Why:

-1-



correctness
run-time

~~MS teams~~

Course

pontis

moodle

TODO

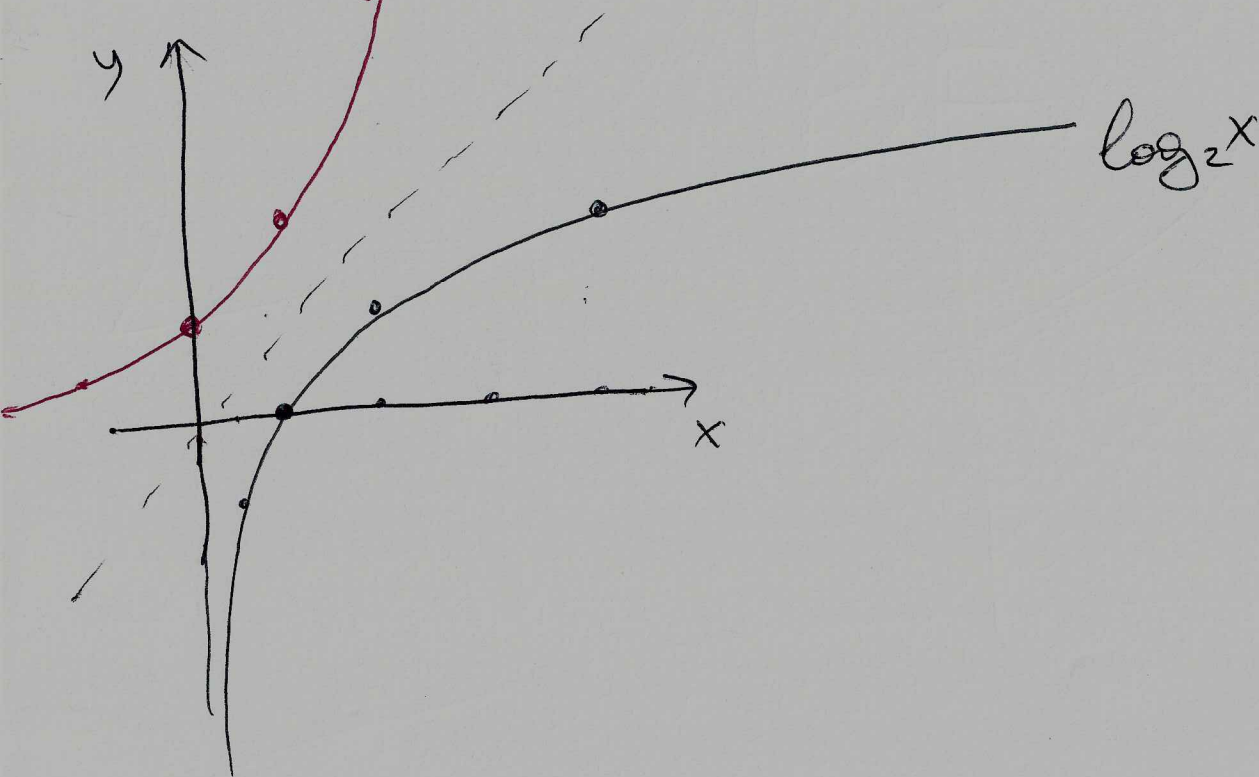
~~MS~~

website: slides, recording,
submissions ←
Q&A

Logarithms

$$\log_b a = c \text{ iff } b^c = a$$

$b > 0, b \neq 1, a > 0$



$$\log_2 4 = 2$$

$$\log_2 2 = 1$$

$$\log_2 1 = 0$$

$$\log_2 \frac{1}{2} = -1$$

$$\log_2 \sqrt{2} = \frac{1}{2}$$

$$\log_2 (-7) \text{ illegal}$$

$$\log_b(b^c) = c$$

$$b^{\log_b a} = a$$

$$\log_b(\exp_b(c)) = c$$

$$\exp_b(\log_b(a)) = a$$

$\sin(x)$
 \sqrt{x}
 x^2
 x^5
 2^x
 \dots
 \log_b
 b^x

$\sin(x)$
 $\text{sqrt}(x)$
 $\text{sq}(x)$
 \dots

-3-

$\log_b(x)$
 $\exp_b(x)$

x^2
 $x \times x$
 user
 unroot
 binary

let's show

$$\log_b(a_1 * a_2) \stackrel{?}{=} \log_b a_1 + \log_b a_2 \quad [\text{since, exponents } 1-1]$$

$$\log_b(a_1 * a_2) \stackrel{?}{=} \log_b a_1 + \log_b a_2 \quad [\text{using } x^{y+z} = x^y * x^z]$$

$$a_1 * a_2 \stackrel{?}{=} b^{\log_b a_1} * b^{\log_b a_2}$$

$$a_1 * a_2 \stackrel{\checkmark}{=} a_1 * a_2$$

-4-
Proof
formal = mathem.

$$\log_b (a_1 \times a_2) = \log_b a_1 + \log_b a_2$$

$$\log_b (a_1 / a_2) = \log_b a_1 - \log_b a_2$$

$$\log_b (a^k) = k \log_b a$$

$$\log_b^k a = \frac{1}{k} \log_b a$$

$$\log_b a = \frac{\log_c a}{\log_c b}$$

$$\rightarrow \log_b a = \frac{\log_a a}{\log_a b} = \frac{1}{\log_a b}$$

$$\log_b n = \frac{\log_{10} n}{\log_{10} b} = \underbrace{\log_b 10}_{\text{constant}} \log_{10} n$$

$$O(\log_b n) = O(\underbrace{\log n}_{\text{no base}})$$

$$\sqrt{\log n}$$

(Base 10)

$$\log_2 3 ?$$

$$\log_2 2 < \log_2 3 < \log_2 4$$

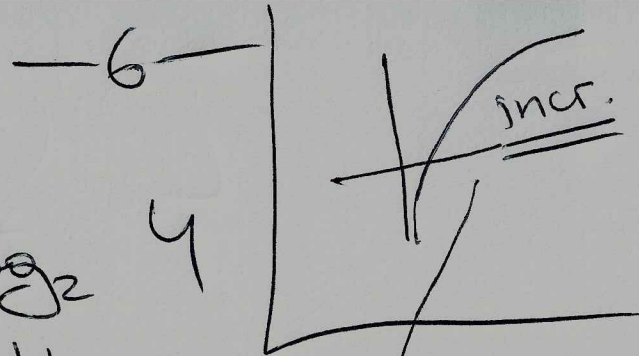
$$1 < \log_2 3 < 2$$

$$1.5 ?$$

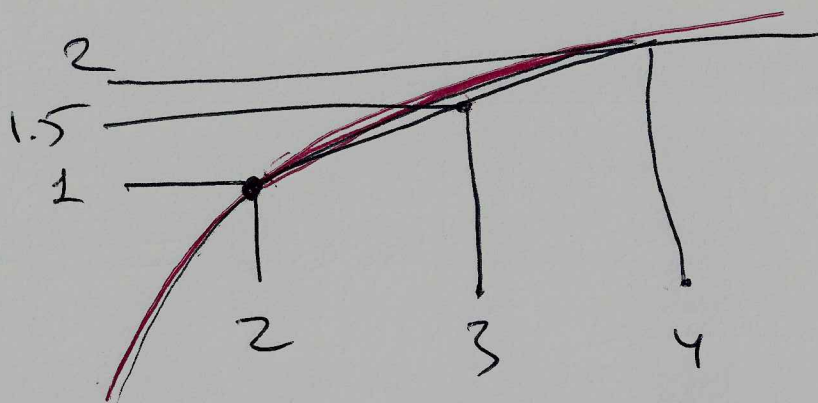
~~"close" = "approx"~~

"less than"

"greater than"



log is "convex up"



$$\log_2 3 \approx 1.58$$

$\log x$ slowest growing "named" function
 $O(\log n) < O(\sqrt[n]{n}) < O(\sqrt{n})$

$$3^{\log_2 n} = 3^{\frac{\log_3 n}{\log_3 2}} = [X^{9/6} = (X^9)^{1/6}] \quad -7-$$

$$= (3^{\log_3 n})^{1/\log_3 2} =$$

$$= n^{\log_2 3} \quad (\text{faster } n^2, \text{ slower than linear})$$