

## HOMEWORK 2

(Math 140)

1. Show that if  $A$  and  $B$  are rotations of  $\mathfrak{R}^2$ , then  $AB = BA$ . Is the same true for rotations in  $\mathfrak{R}^3$ ? (20 pts)

2. Given  $A = \begin{pmatrix} 1 & -1 & 0 \\ 2 & -3 & 2 \\ 0 & 1 & -1 \end{pmatrix}$ , find  $A^{-1}$ . (20 pts)

3. Let  $A$  be a  $3 \times 3$  matrix. Show that  $|cA| = c^3|A|$ . (20 pts)

4. Rotation of a figure about a point  $P$  in  $\mathfrak{R}^2$  is accomplished by first translating the figure by  $-P$ , rotating about the origin, and then translating back to  $P$ . Construct a  $3 \times 3$  matrix  $A$  that rotates points by  $45^\circ$  about the point  $(1,2)$ , using homogeneous coordinates. (20 pts)

5. Given the basis  $A = \begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$ ,  $B = \begin{pmatrix} 0 & 1 \\ 0 & -1 \end{pmatrix}$ ,  $C = \begin{pmatrix} 0 & 0 \\ -2 & 1 \end{pmatrix}$ ,  $D = \begin{pmatrix} 0 & 0 \\ 0 & 2 \end{pmatrix}$ , examine whether it is an orthonormal basis. If your answer is **no**, then use the *Gram-Schmidt Orthogonalization Process* to construct an orthonormal basis out of the one above. (20 pts)